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#### Numerical Simulation of Cyclic Seaward Bar Migration

Yoshiaki KURIYAMA\*

#### **Synopsis**

A one-dimensional model for beach profile change was developed to predict cyclic longshore bar evolutions. The cross-shore sediment transport was assumed to be composed of suspended load due to wave breaking and bed load due to velocity skewness, velocity atiltness, and beach slope. The model was calibrated with beach profile data obtained every weekday at 5-m intervals along a 400-m-long pier at the Hazaki Oceanographical Research Station, located on the Hasaki coast of Japan, during a 1-year period from January to December 1989. The optimal values of the parameters included in the cross-shore sediment transport rate formula and the smoothing number for suspended load were obtained so that the error function that was the sum of the errors in elevation and bar crest position was minimal. The model with the optimal parameter set and the optimal smoothing number was applied to the bar migrations during a period of 2 years, including the 1-year calibration period of 1989 and the following year of 1990. The predicted bar crest positions agreed well with the measured positions, and the Brier skill score was over 0.5 in the bar-trough zone at the end of the 2-year calculation. The model was also applied to bar evolutions outside the calibration period, during the period from 1991 to 2000, which was divided into five 2-year blocks. With the exception of the block representing 1999 to 2000, the model qualitatively reproduced cyclic bar migrations.

Key Words: bar migration, bar evolution, bed load, cross-shore sediment transport, longshore bar, numerical model, suspended load

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沿岸砂州の繰り返し沖向き移動に関する数値計算

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要 旨

沿岸砂州の繰り返しの沖向き移動を推定するために、断面変化に関する数値シミュレーションモ デルを構築した.モデルは砕波によって浮遊した底質が戻り流れにより沖向きに輸送される浮遊砂 量および流速の非線形性による岸向きの掃流砂量,海底勾配による掃流砂量を考慮している.モデ ルに含まれる漂砂量の係数を,茨城県波崎海岸でほぼ毎日観測された1989年の1年間の断面変化を 基に決定するとともに、モデルの現地適用性をキャリブレーション期間を含む1989年~1990年の2 年間およびそれ以外の期間である1991年~2000年の10年間の現地データで検証した.その結果、 モデルはキャリブレーション期間を含む約2年間の繰り返しの沖向き移動を定量的に再現でき、そ れ以外の期間についても、定性的には繰り返しの砂州移動を再現できた.

キーワード:沿岸砂州,砂州移動,岸沖漂砂量,浮遊砂,掃流砂,数値モデル

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#### 1. Introduction

Longshore bars are frequently observed on sandy beaches, and migrate seaward and shoreward in the short term (shorter than several weeks). However, medium-term (several weeks to 10 years) and long-term (longer than 10 years) bar migrations are more frequently in the seaward direction (e.g., Birkemeier, 1984; Lippmann et al., 1993; Ruessink and Kroon, 1994; Wijnberg and Terwindt, 1995; Shand and Bailey, 1999; Shand et al., 1999; Kuriyama, 2002; Ruessink et al., 2003; Kuriyama et al., 2008a).

Bars significantly influence currents and morphological variations in the nearshore zone. Although the shoreline normally retreats during a storm and recovers after the storm, laboratory experiments by Yamamoto and Sato (1998) demonstrated that the shoreline did not recover during a mild wave condition when the offshore bar formed during the preceding severe wave condition was removed. Coastal ecological systems are also influenced by bars. Higano (1994) showed that the predominant species of bivalves differ on the shoreward and seaward sides of a longshore bar. Therefore when we deal with morphological and ecological problems of sandy beaches, predicting bar migrations is strongly required.

To simulate medium-term bar migrations, numerous models have been proposed. Some of the models could predict a part, or in some cases the whole, cycle of bar evolution consisting of generation, seaward migration and decay. However, the durations of bar evolution cycles are longer than the periods investigated when testing model validity; therefore, the ability of models to reproduce cyclic bar evolutions has not been fully examined. The objective of this study was to develop a process-based one-dimensional model for beach profile change and to investigate the validity of the simulated cyclic bar evolutions using daily field measurements of beach profiles.

#### 2. Previous studies

A model for predicting the locations of bar crest was developed by Plant et al. (1999), who assumed that a bar migrates toward a wave height-dependent equilibrium point and that the migration rate is proportional to the wave height and the distance between the present bar crest location and the equilibrium one. They applied their model to bar migration at Duck, North Carolina, USA, and showed that the model successfully predicted bar migration over an interval of 7 years. The model was expanded by Pape et al. (2009a), who demonstrated that the model reasonably reproduced bar crest movements over an interval of about 8 years at the Gold Coast, Australia, and Egmond, the Netherlands.

Pape et al. (2007) and Pape et al. (2009b) developed another model for bar crest movement using a neural network. The model worked well for bar crest movement on the Gold Coast over about 2 years. However, on the Hasaki coast, Japan, where the duration of seaward bar migration is about 1 to 2 years, while some of the bar crest movements were predicted well by the model, some others were not, and the overall model performance over an interval of 15 years was concluded to be relatively poor.

A method of predicting not only the bar crest position but also bar evolution is to estimate the elevation change on the basis of the spatial gradient of the cross-shore sediment transport rate. Gallagher et al. (1998) predicted bar migration at Duck over about 2 months using the cross-shore sediment transport rate formula proposed by Bailard (1981) and substituting velocities measured in the field into the formula. The result showed that seaward bar migration was predicted well using this method but that the shoreward migration was not. Hoefel and Elgar (2003) improved the model by adding a term related to the acceleration skewness and successfully reproduced both seaward and shoreward bar migrations.

Plant et al. (2004) developed a process-based model in which the cross-shore sediment transport rate was assumed to be a quadratic function of the wave height to water depth ratio as in the earlier study of Plant et al. (2001). The model was applied to a bar migration at Duck over about 1 month, but the model performance was relatively poor. Marino-Tapia et al. (2007a) predicted bar migrations at Duck using Bailard's (1981) cross-shore sediment transport rate formula and substituting the shape functions developed by Mario-Tapia et al. (2007b) into the terms of the third and fourth power of velocity. The bar crest movement predicted by the model for a 77-day interval fitted that measured in the field reasonably well.

van Rijn et al. (2003) compared short- and medium-term beach profile changes measured on a barred beach at Egmond with those predicted by several process-based models. They showed that the two models, UNIBEST and CROSMOR, worked well for the outer bar migration over about 4 months but not for inner bar migration and the beach profile change in the foreshore.

Using the UNIBEST model, Ruessink et al. (2007) successfully reproduced bar migrations at Hasaki, Duck and Egmond over intervals of 10 days to 4 months. Furthermore, Ruessink and Kuriyama (2008) investigated the performance of the UNIBEST model for bar migration at Hasaki over 18 months; the results showed that the performance of this model was high for the first 15 months but rapidly decreased after this time. Pape et al. (2009b) also investigated the performance of the UNIBEST model for bar migration at Hasaki during the period from 1987 to 2001, which was divided into 16 blocks, each of which included a series of bar migrations. The results showed that even with optimal parameter sets for each block, the model performance was variable with some poor results. Walstra and Ruessink (2009) demonstrated that the UNIBEST model predicted the bar development and decay at Noordwijk, the Netherlands, over 3 years, although the field data used for the model validation were not obtained for the same interval as the prediction.

#### 3. Data description

The model developed in this study was compared with beach profile data obtained at Hazaki Oceanographical Research Station (HORS). HORS is located on the Hasaki coast of Japan facing the Pacific Ocean (Figure 1) and has a 400-m-long pier. The beach profiles along the pier have been measured every weekday at 5-m intervals since 1986 using a 5-kg lead weight from the pier and a level and staff shoreward of the pier. The median sediment diameter along the profile is 0.18 mm, and it remains almost uniform along the profile (Katoh and Yanagishima, 1995). The bathymetry around the pier is almost uniform alongshore according to Kuriyama (2002), who applied Empirical Orthogonal Function analysis to 17 bathymetric maps around HORS obtained from 1986 to 1998. Based on the datum level at Hasaki (Tokyo Peil -0.687 m), the high, mean and low water levels are 1.25 m, 0.65 m, and -0.20 m, respectively, and the tidal range is 1.45 m. Wind angle and velocity were measured at the tip of the pier for 10 minutes every hour. Deepwater waves were measured at a water depth of about 24 m with an ultrasonic wave gage for 20 minutes every 2 hours (see location on Figure 1).

**Figure 2** shows the mean beach profiles during the period from 1987 to 2001. Each position along the pier is referred to by its seaward distance relative to the reference point located



Figure 1 Locations of HORS and the wave gage.



**Figure 2** Mean beach profile from 1987 to 2001 based on daily measurements along the HORS pier (thick line) and yearly bathymetric surveys around HORS (thin line). The elevation is based on the Hasaki datum level.

close to the pier entrance and designated as "P." For example, P230m denotes a position 230 m seaward from the reference point. The mean beach slope decreases gradually offshore. Gradients are about 1/40 near the shoreline at the low water level, about 1/80 at P250m, and about 1/110 near the tip of the pier. Longshore bars are frequently observed in the area between P180m and P380m, and they move seaward with durations of 1 to 2 years (Kuriyama et al., 2008a).

#### 4. Numerical model

The one-dimensional numerical model for bar evolution developed in this study is composed of five sub-models for wave and surface roller transformation, undertow velocity, longshore current velocity, velocity skewness and atiltness, and beach profile change. The sub-models for wave and surface roller transformation, undertow velocity and longshore current velocity are based on those of Kuriyama (2010a).

#### 4.1 Wave and surface roller transformation

The wave and surface roller transformation sub-model estimates the cross-shore variation of the root-mean-square wave height  $H_{rms}$ , which is used in estimating the undertow and longshore current velocities and sediment transport rates in the following sub-models. A Rayleigh distribution is assumed as the wave height probability density function over an entire computational domain, following Thornton and Guza (1983). The energy of waves with heights larger than the breaking wave height is dissipated.

The breaking wave height is estimated with Equation (1), as proposed by Seyama and Kimura (1988).

$$\frac{H_b}{h_b} = C_{br} [0.16 \frac{L_0}{h_b} \left\{ 1 - \exp\left[ -0.8\pi \frac{h_b}{L_0} \left( 1 + 15 \tan^{4/3} \beta \right) \right] \right\}$$
  
- 0.96 \tan \beta + 0.2]

(1)

where  $H_b$  is the breaking wave height,  $h_b$  is the breaking water depth,  $C_{br}$  is a nondimensional coefficient,  $L_0$  is the offshore wavelength and  $\tan\beta$  is the beach slope. The nondimensional coefficient  $C_{br}$  was introduced by Kuriyama (1996) to fit experimental data-based Equation (1) to field data. The beach slope is defined as positive for water depth increasing seaward and estimated as the average slope in a 30-m-long region for which the definition point is located at the center.

Wave energy dissipation is estimated using the periodic bore model proposed by Thornton and Guza (1983) and 20 representative wave heights raging from  $H_b$  to  $3H_b$ .

$$\frac{\partial E_w C_g \cos\theta}{\partial x} = \int_{H_b}^{\infty} P(H)B(H)dH$$

$$B(H) = \frac{1}{4}\rho g \frac{1}{T} \frac{(B_w H)^3}{h}$$
(2)

where  $E_w$  is the wave energy,  $C_g$  is the group velocity,  $\theta$  is the

wave direction, x is the seaward distance, P(H) is the probability density of the wave height,  $\rho$  is the seawater density, g is the gravitational acceleration, T is the wave period, H is the wave height and h is the water depth. A nondimensional parameter  $B_w$  was formulated as in Equation (3) of Kuriyama and Ozaki (1996) using Seyama and Kimura's (1988) experimental data.

$$B_W = C_B \left\{ 1.6 - 0.12 \ln(H_0 / L_0) + 0.28 \ln(\tan \beta) \right\}$$
(3)

where  $H_0$  is the offshore wave height and  $C_B$  is a nondimensional coefficient.

The calculation uses the peak wave period as the wave period, following Grasmeijer and Ruessink (2003). The significant wave height  $H_{1/3}$  is estimated as  $H_{1/3} = 1.416 H_{rms}$ .

The development and decay of a surface roller in the surf zone is estimated on the basis of the energy balance following Kuriyama (2010a), who assumed that the vertical distribution of the cross-shore velocity in a surface roller is triangular with the celerity C at the top of the roller and zero at the bottom, as described by Kuriyama and Nakatsukasa (2000).

$$\frac{\partial (E_w C_g \cos \theta)}{\partial x} + \frac{\partial (F_r \cos \theta)}{\partial x} = D_r, \quad F_r = \frac{1}{8}\rho C^3 \frac{A_r}{L}$$

$$D_r = B_r \frac{gF_r}{C^2} \frac{A_r}{h^2}$$
(4)

where  $F_r$  is the surface roller energy flux,  $D_r$  is the energy dissipation rate of a surface roller,  $A_r$  is the area of a surface roller and  $B_r$  is a nondimensional coefficient, which was set to be 0.096 according to Kuriyama (2010a).

#### 4.2 Undertow velocity

The vertically averaged undertow velocity U is estimated from Equation (5) from Svendsen (1984).

$$U = \frac{Q_w + Q_r}{d_{tr}} \tag{5}$$

where  $Q_w$  and  $Q_r$  are the mass fluxes due to waves and surface rollers, respectively. The value of  $d_{tr}$  represents the distance between the wave trough level and the bottom, and is assumed to be  $d_{tr} = h - H/2$ .

Equation (6), which was also proposed by Svendsen (1984), is used to estimate  $Q_w$ .

$$Q_w = \frac{C}{h} \zeta_{rms}^2 \tag{6}$$

where  $\zeta_{rms}$  is the standard deviation of the water surface elevation of a wave, which is obtained from Equation (7) with

(7)

the parameter  $\Pi$  for wave nonlinearity proposed by Goda (1983).

$$\begin{aligned} \zeta_{rms} &= \frac{1}{2\sqrt{2}} H_{rms}, & \Pi < 0.15 \\ \zeta_{rms} &= \frac{1}{1.668 \log_{10} \Pi_{rms} + 4.204} H_{rms}, & 0.15 \le \Pi < 3 \\ \zeta_{rms} &= \frac{1}{5} H_{rms}, & \Pi \ge 3 \end{aligned}$$

with 
$$\Pi = \frac{H_{rms}}{L} \tanh^3 \frac{2\pi h}{L}$$
 (8)

where L is the wavelength.

The value of  $Q_r$  is estimated as follows:

$$Q_r = \frac{A_r C}{2L} \tag{9}$$

#### 4.3 Longshore current velocity

The vertically averaged longshore current velocity V is estimated from Equation (10), which represents the momentum balance among the gradient of the radiation stress  $R_x$ , the wind stress  $W_x$ , the gradient of the momentum flux due to a surface roller  $M_x$ , the lateral mixing term  $L_x$  and the bottom friction  $F_x$ .

$$R_{\chi} - W_{\chi} + M_{\chi} - L_{\chi} + F_{\chi} = 0 \tag{10}$$

The gradient of the radiation stress term  $R_x$  is estimated using small-amplitude wave theory.

$$R_x = \frac{1}{\rho h} \left( \frac{\partial S_{yx}}{\partial x} \right), \quad S_{yx} = \rho g \frac{C_g}{C} \frac{1}{8} H_{rms}^2 \cos \theta \sin \theta$$
(11)

The wind stress  $W_x$  is assumed to be

$$W_x = \frac{1}{\rho h} C_d \rho_a W_v^2 \sin \alpha_w \tag{12}$$

where  $C_d$  is a nondimensional coefficient,  $\rho_a$  is the air density,  $W_v$  is the wind velocity, and  $\alpha_w$  is the wind direction. The value of  $C_d$  was assumed to be 0.0022 following Kuriyama et al. (2008b).

The gradient of the momentum flux due to a surface roller  $M_x$  is expressed as

$$M_x = \frac{1}{\rho h} \left( \frac{\partial M_r}{\partial x} \right), \quad M_r = -\frac{1}{3} \rho_w C^2 \frac{A_r}{L} \cos \theta \sin \theta \quad (13)$$

The lateral mixing term  $L_x$  is assumed, as in the study of Ruessink et al. (2001), with a dimensional coefficient v.

$$L_{x} = \frac{\partial}{\partial x} \left( \varepsilon \frac{\partial V}{\partial x} \right), \quad \varepsilon = vh \tag{14}$$

The bottom friction  $F_x$ , as proposed by Nishimura (1988),

is used in the model.

$$F_{x} = \frac{C_{f}}{h} (W + \frac{w_{b}^{2}}{W} \sin^{2} \theta) V$$

$$W = \frac{\sqrt{V^{2} + w_{b}^{2} + 2Vw_{b} \sin \theta} + \sqrt{V^{2} + w_{b}^{2} - 2Vw_{b} \sin \theta}}{2}$$

$$w_{b} = \frac{2v_{m}}{\pi}, \quad v_{m} = \frac{\pi H_{rms}}{T \sinh(\frac{2\pi h}{L})}$$
(15)

where  $C_f$  is a nondimensional coefficient and  $u_{b,rms}$  is the amplitude of orbital near-bottom velocity. Following Garcez-Faria et al. (1998) and Ruessink et al. (2001), the friction coefficient  $C_f$  is assumed to be a function of the water depth as expressed by Equation (16) with the apparent bed roughness  $k_a$ .

$$C_f = 0.015 \left(\frac{k_a}{h}\right)^{1/3}$$
 (16)

#### 4.4 Velocity skewness and atiltness

In the beach profile change sub-model mentioned later, velocity and acceleration asymmetries are taken into account although the wave and surface roller transformation sub-model mentioned above cannot predict their properties. Hence, this section discusses how to estimate the velocity and acceleration asymmetries.

As parameters representing the velocity and acceleration asymmetries, velocity skewness  $(\sqrt{\beta_1})_u$  and velocity atiltness  $(\beta_3)_u$ , which was proposed by Goda (1985), were chosen.

$$\left(\sqrt{\beta_1}\right)_{u} = \frac{\frac{1}{N} \sum_{i=1}^{N} (u_i - \overline{u})^3}{u_{rms}^3}, \quad u_{rms} = \frac{1}{N} \sum_{i=1}^{N} (u_i - \overline{u})^2 \quad (17)$$

$$(\beta_3)_u = \frac{\frac{1}{N-1} \sum_{i=1}^{N-1} (a_i - \overline{a})^3}{a_{rms}^3}, \quad a_i = \frac{u_{i+1} - u_i}{\Delta t}$$

$$a_{rms} = \frac{1}{N-1} \sum_{i=1}^{N-1} (a_i - \overline{a})^2$$
(18)

where *u* is the fluid velocity, *a* is the acceleration and *N* is the data number. The overbar denotes the average value.

On the basis of fluid velocities measured in the surf zone at HORS, Kuriyama et al. (1990) and Kuriyama (1991) proposed Equations (19) and (20) for estimating velocity skewness and atiltness from  $\Pi_{1/3}$ , which is a wave

nonlinearity parameter proposed by Goda (1983) and is a function of the wave height, wavelength, and water depth (Equation (21)).

$$\begin{pmatrix} \sqrt{\beta_1} \\ u \\ \sqrt{\beta_1} \\ u \\ = 0.36, \\ (19) \\ (\beta_3)_u = 1.03\Pi_{1/3} + 0.76, \\ (19) \\ 0.4 \le \Pi_{1/3} < 2 \\ 0.3 \le \Pi_{1/3} < 2 \\ (20) \\ 0.3 \le \Pi_{1/3} < 2 \\ (2$$

$$\Pi_{1/3} = \frac{H_{1/3}}{L_{1/3}} \coth^3 \frac{2\pi h}{L_{1/3}}$$
(21)

where  $L_{1/3}$  is the wavelength corresponding to the significant wave period.

Goda (1983) showed that the skewness of surface waves is proportional to  $\Pi_{1/3}$  when  $\Pi_{1/3} < 0.15$ . Doering and Bowen (1995) proposed formulae for estimating wave skewness and asymmetry using the Ursell parameter. On the basis of these findings,  $\left(\sqrt{\beta_1}\right)_u$  and  $(\beta_3)_u$  were assumed to be expressed by Equations (22) and (23), respectively, and the coefficients of  $c_1$  to  $c_5$  were determined so that Equations (22) and (23) fit well with Equations (19) and (20), respectively.

$$\left( \sqrt{\beta_1} \right)_{\mathcal{U}} = c_1 \Pi_{1/3}, \qquad \Pi_{1/3} < 0.15$$

$$\left( \sqrt{\beta_1} \right)_{\mathcal{U}} = \left[ c_2 + c_3 \log(\frac{3\pi}{4} \Pi_{1/3}) \right]$$

$$\cos \left\{ \left[ -90 + 90 \tanh(0.73 \frac{4}{3\pi \Pi_{1/3}}) \frac{\pi}{180} \right] \right\}, 0.15 \le \Pi_{1/3}$$

$$(22)$$

$$(\beta_3)_u = \left[c_4 + c_5 \log \log(\frac{3\pi}{4}\Pi_{1/3})\right]$$

$$\cos\left\{\left[-90 + 90 \tanh(0.73\frac{4}{3\pi\Pi_{1/3}})\frac{\pi}{180}\right]\right\}$$
(23)

The obtained values of  $c_1$  to  $c_5$  are 0.86, 0.54, 0.90, -0.67, and -0.56. Comparisons between Equations (22) and (19) and between Equations (23) and (20) show that Equations (22) and (23) represent the velocity skewness and atiltness in the field well (**Figure 3**).

#### 4.5 Beach profile change

Change in the beach profile is estimated on the basis of a continuity equation (Equation (24)) and the cross-shore gradient of the cross-shore sediment transport rate. The



**Figure 3** (a) Relationship between velocity skewness and  $\Pi_{1/3}$ . The solid and broken lines represent Equations (22) and (19), respectively. (b) Relationship between velocity atiltness and  $\Pi_{1/3}$ . The solid and broken lines represent Equations (23) and (20), respectively.

alongshore gradient of the longshore sediment transport rate is assumed to be negligible.

$$\frac{\Delta z}{\Delta t} = -\frac{1}{1-\lambda} \frac{\Delta Q}{\Delta x}$$
(24)

where z is the elevation, which is positive in the upward direction, t is the time,  $\lambda$  is the porosity (= 0.3), and Q is the cross-shore sediment transport rate, which is positive in the seaward direction, per unit length in the alongshore direction.

The cross-shore sediment transport rate is assumed to be made up of four contributions due to sediment suspension and undertow  $Q_s$ , near-bottom velocity skewness and amplitude  $Q_{b,v}$ , near-bottom acceleration skewness  $Q_{b,a}$  and beach slope  $Q_{b,slope}$ .

The value of  $Q_s$  is expressed in Equation (25) on the basis of the assumption that the amount of suspended sediments is proportional to the surface roller energy dissipation rate, as assumed by Kobayashi et al. (2008).

$$Q_s = \alpha_1 \frac{D_r}{\rho g(s-1)w_f} U \tag{25}$$

where  $\alpha_1$  is a coefficient, s is the sediment specific gravity

and  $w_f$  is the sediment fall velocity.

The spatial distribution of suspended sediment transport rate in the field is expected to be smoother than that of  $Q_s$  as estimated by Equation (25) due to the effects of advection and diffusion of suspended sediment, which are not included in the present model. Thus, the spatial distribution of  $Q_s$  as estimated by Equation (25) is smoothed by the triangular filter expressed by Equation (26). The smoothing number was determined in the calibration described below.

$$Q_{s,i,m} = (Q_{s,i-1,m-1} + 2Q_{s,i,m-1} + Q_{s,i+1,m-1})/4 \quad (26)$$

where i is the grid number and m is the smoothing number.

On the basis of Bailard's (1981) formula, the value of  $Q_{b,v}$  is assumed to be

$$Q_{b,v} = -\alpha_2 ((\sqrt{\beta_1})_u u_{b,rms}^3 \cos \theta + (u_{b,rms}^2 + u_{bl,rms}^2)V \sin \theta \cos \theta)$$
(27)

where  $\alpha_2$  is a coefficient (s<sup>2</sup>/m) and  $u_{bl,rms}$  is the amplitude of long-period near-bottom velocity, which is estimated on the basis of Goda (1975) using Equation (28).

$$u_{bl,rms} = 0.01 \sqrt{g/h} \left[ 1/\sqrt{(H_0/L_0)(1+h/H_0)} \right] H_0$$
 (28)

Bailard's (1981) formula includes terms related to the near-bottom time-averaged velocity. The near-bottom time-averaged velocity in the surf zone is seaward and relatively large, but its accurate prediction is still a great challenge, despite several methods having been proposed (e.g., Garcez-Faria et al., 2000; Reniers et al., 2004). Hence, in this study,  $Q_{b,v}$  is assumed not to include a term for sediment transport rate due to the near-bottom time-averaged velocity, which may be counted in  $Q_s$ .

The value of  $Q_{b,a}$  is expressed by Equation (29), as given by Hoefel and Elgar (2003).

$$Q_{b,a} = -\alpha_3 \left( (\beta_3)_u a_{b,rms} - a_{cr} | (\beta_3)_u | / (\beta_3)_u \right) \cos \theta,$$
  
$$\left| (\beta_3)_u a_{b,rms} | > a_{cr} \quad (29) \right.$$
  
$$Q_{b,a} = 0, \qquad \qquad \left| (\beta_3)_u a_{b,rms} \right| \le a_{cr}$$

where  $\alpha_3$  is a coefficient (m s),  $a_{r,rms}$  is the amplitude of near-bottom acceleration and  $a_{cr}$  is a threshold value (= 0.2 m/s<sup>2</sup>).

The value of  $Q_{b,slope}$  is also based on that of Bailard (1981).

$$Q_{b,slope} = \alpha_4 \frac{\tan\beta}{\tan\phi} \left( u_{b,rms}^3 + u_{bl,rms}^3 \right)$$
(30)

where  $\alpha_4$  is a coefficient (s<sup>2</sup>/m) and  $\phi$  is the internal friction angle of the sediment (= 30 degrees). Although

Bailard (1981) assumed  $\alpha_4$  was equal to  $\alpha_2$ ,  $\alpha_4$  in this study is assumed to be different from  $\alpha_2$ .

#### 5. Calibration

The parameters  $\alpha_1$  to  $\alpha_4$  included in the equations representing the four types of cross-shore sediment transport rates and the smoothing number for the suspended load were determined from beach profile data obtained at HORS between January and December 1989.

#### 5.1 Model setup

The cross-shore grid size was set at 5 m, and the time interval was 2 hours. The seaward boundary was set at P1200m, where the elevation was -10.7 m based on the Hasaki datum level. The input data at the seaward boundary were the wave heights and periods estimated from values measured with the wave gage at a water depth of about 24 m (see location on **Figure 1**), the wave angles estimated by Hashimoto et al. (2000) using WAM, a third generation wave prediction model, and the estimated astronomical tide levels.

The initial beach profile shoreward of P385m was set as the profile measured on January 4, 1989, and that seaward of P445m was set as the mean beach profile shown in **Figure 2**. The profile between P390m and P440m was interpolated from the elevations at P385m and P445m.

The values of  $C_{br}$  and  $C_B$  in Equations (1) and (3) were set to 0.70 and 0.75, respectively, so that the error between the significant wave heights measured (Kuriyama et al., 2008b) and predicted along the HORS pier during the period from 1987 to 2001 was minimal. The values of  $\nu$  in Equation (14) and  $k_a$  in Equation (16) were set at 5.0 m<sup>2</sup>/s and 0.15 m as used by *Kuriyama* (2010b) for HORS long-term longshore current velocity data.

The parameters in the cross-shore sediment transport rate formulae (Equations (25), (27) and (29)) and the smoothing number for the suspended load were determined so that the error function described below was minimal using SCE-UA algorism (Shuffled Complex Evolution – University of Arizona) (Duan et al., 1993) as in the study of Ruessink et al. (2007). The error function F in the calibration was set as the sum of the relative errors in elevation and bar crest position, which are represented by the first and second terms of the right-hand side of Equation (31).

$$F = \frac{\sum_{x,t} (z_p(x,t) - z_m(x,t))^2}{\sum_{x,t} (z_m(x,t) - z_m(x,0))^2} + \frac{\sum_t (x_{c,p}(t) - x_{c,m}(t))^2}{\sum_t (x_{c,m}(t) - 180)^2}$$
(31)

where  $x_c$  is the bar crest position and the subscripts p and m denote the predicted and measured values, respectively. The locations of the bar crest and trough were defined as the points where the beach slope changes, looking offshore, from a negative value to a positive value and vice versa. A bar was defined in this study as one with a bar height (the difference between the elevations at the crest and the shoreward trough) larger than 0.5 m. The baseline prediction for the relative error in elevation is the initial beach profile and that in bar crest position is P180m, where most bars at Hasaki were generated and started to migrate seaward. The second term of Equation (31) is calculated when a bar is observed in the measurement. The second term was added into the error function because there is a possibility that the first term cannot precisely evaluate the model performance in the bar migration direction as suggested by van Rijn (2003).

#### 5.2 Calibration result

The optimal parameters obtained were  $\alpha_1 = 1.147 \text{ x } 10^{-3}$ ,  $\alpha_2 = 7.651 \text{ x } 10^{-4} (\text{s}^2/\text{m})$ ,  $\alpha_3 = 9.96 \text{ x } 10^{-5} (\text{m s})$  and  $\alpha_4 = 7.755 \text{ x } 10^{-4} (\text{s}^2/\text{m})$ , and the smoothing number was 15. The relative errors in elevation and bar crest position, represented by the first and second terms of the right-hand side of Equation (31), were 0.609 and 0.093, respectively.

The model closely predicted the bar crest positions for almost 2 years including the 1-year calibration period of 1989 and the following year of 1990 (**Figures 4 and 5**); the input offshore significant wave height and period are shown in **Figure 6**. The seaward bar migration from January 1989 and the generation of a new bar at P200m at the end of 1989 were well predicted in the model. Even in 1990, after the calibration period, although the predicted bar crest location was slightly shoreward of the measured one, the model successfully predicted the seaward bar migration between January and April and the shoreward migration between April and September.

The model also performed well with respect to the changes in the beach profile (**Figure 7**). The predicted bar crest location and elevation agreed well with field measurements taken in 1989, although the model performed less well in the



**Figure 4** Time series of measured (solid circles) and predicted (open circles) bar crest positions. The solid lines show the series of bar migrations.



**Figure 5** Spatial and temporal variations of measured (a) and predicted (b) elevations on the basis of the mean beach profile (**Figure 2**). Elevations above and below the mean beach profile are indicated by warm and cold colors, respectively. The horizontal broken line in (b) shows the location of the tip of the pier. See **Figure 5** for further explanation.

foreshore than in the bar-trough zone. In 1990, the predicted location of the bar crest was shoreward of the measured one as mentioned above, which resulted in an increase in the discrepancy between the prediction and measurement. After November 1990, the predicted profile became flat and the bar was not prominent.

The model performance mentioned above is reflected in the Brier skill score *BSS* (Murphy and Epstein, 1989), defined by Equation (32). The value of *BSS* is equal to 1 when the



**Figure 6** Input offshore significant wave height (a) and period (b) during the period from 1989 to 1990.

prediction perfectly matches the measurement and falls below 0 when the model performance is poorer than the model that assumes no change.

$$BSS = 1 - \frac{\sum_{x,t} (z_p(x,t) - z_m(x,t))^2}{\sum_{x,t} (z_m(x,t) - z_m(x,0))^2}$$
(32)

The *BSS* value was above 0 in the region between P-65m and P355m, which includes the foreshore, inner surf zone and bar-trough zone, by the middle of December 1990, and over 0.5 in the bar-trough region (P205m to P535m) at the end of 1990 (**Figure 8**). This result indicates that the model well reproduced the cyclic bar migrations for an interval of about 2 years including the 1-year calibration period.



Figure 7 Measured (broken lines) and predicted (solid lines) beach profiles. (The broken lines show the initial beach profile on January 4, 1989.)



**Figure 8** Time series of the model skill score *BSS* in the region from P-65 m to P355 m (solid line) and that from P205m to P355m, the bar-trough region (broken line).

#### 6. Application for bar migrations from 1991 to

#### 2000

The model performance outside the calibration period was examined by comparing the beach profile data obtained during a 10-year period from January 1991 to December 2000. The period was divided into five 2-year blocks. The input offshore significant wave heights and periods during this interval are shown in **Figure 9**.

The *BSS* value in the bar-trough zone was higher than that in the whole region (**Figure 10**) as was the case for the calibration period, and the *BSS* value in the bar-trough region was above 0 at the end of the calculations for three of the five blocks.

During the period from 1991 to 1992, the prediction successfully reproduced the seaward bar migration occurring from January 1991 and a new bar formation at around P190m in October 1991 as well as its subsequent seaward migration (**Figures 11 (a), 12 (a) and 12 (f)**). However, the bars and troughs were more developed in the prediction than in the measurement, which resulted in *BSS* values below 0 in the bar-trough region from October 1991 (**Figure 10**).

The model also reproduced the seaward bar migration from January 1993 and a new bar formation at around P185m in April 1993 (Figures 11 (b), 12 (b) and 12 (g)). Subsequently, however, the bar in the model prediction decayed and the bar height fell to lower than 0.5 m, which was not compatible with the field observations.

As shown in Figures 11 (c), 12 (c) and 12 (h), although the seaward bar migration from January 1995 was reproduced in



**Figure 9** Input offshore significant wave height (a) and period (b) during the period from 1991 to 2000.



**Figure 10** Time series of *BSS* for the regions from P-65m to P355m (a) and from P205m to P355m (bar-trough zone) (b). The black, solid red, broken red, solid blue, broken blue and green lines show the values during the periods from 1991 to 1992, from 1993 to 1994, from 1995 to 1996, from 1997 to 1998, and from 1999 to 2000.



**Figure 11** Bar crest positions measured and predicted during the periods from 1991 to 1992 (a), from 1993 to 1994 (b), from 1995 to 1996 (c), from 1997 to 1998 (d), and from 1999 to 2000 (e). See **Figure 4** for further explanation.

the model prediction, the migration rate was faster in the prediction than that in the measurement and the location of the bar in the model prediction was seaward of that in the measurement.

During the period from 1997 to 1998, the model predicted a flatter beach profile than that which was measured (**Figures 12 (d) and (i)**) and did not predict the formation of bars, which are defined here as those with heights greater than 0.5 m (**Figure 11 (d)**). However, at around P320m during the period from January to September 1997 and at around P200m during the period from October to December 1997, where and when bars were formed in the measurement, the model predicted elevations higher than the mean beach profile (**Figures 12 (d) and (i)**).

The *BSS* value was much lower during the 1999-2000 interval, both in the bar-trough region and the whole region, than in the other intervals (**Figure 10**). The reason for this is that the model could not reproduce the changes in the beach profile including seaward bar migration and new bar formation between March 15 and 25 in 1999 (**Figures 11 (d)**, **12 (d) and 12 (j)**), during which time two storms with wave heights exceeding 3.0 m attacked the beach although such wave heights during a storm were not unusually large. The reason for this discrepancy between the predicted and measured profiles is still unclear.

As mentioned above, even when the predicted profile does not technically contain a bar because the bar height is smaller than 0.5 m, an area above the mean beach profile is sometimes formed in the model prediction at around the bar crest position in the measurement. In this case, it appears that the model is capable of predicting bar migrations not quantitatively but qualitatively. Hence, the centers of areas that are 0.2 m higher than the mean beach profile and have cross-shore lengths longer than 20 m were compared in the prediction and measurement.

Except for the period from 1999 to 2000, the centers of the accumulation areas in the prediction and measurement agree well (**Figure 13**) and the Brier skill scores for the centers of accumulation areas  $BSS_c$ , defined by Equation (33), are mostly above 0 (**Figure 14**). This result indicates that the model in this study predicted cyclic bar evolutions during an 8-year period from 1991 to 1998 (i.e., outside the calibration period) at least qualitatively.

$$BSS_{c} = 1 - \frac{\sum_{t} \left( X_{c,p}(t) - X_{c,m}(t) \right)^{2}}{\sum_{t} \left( X_{c,m}(t) - X_{c,m}(0) \right)^{2}}$$
(33)

where  $X_c$  is the center of an area above the mean beach profile.



**Figure 12** Spatial and temporal variations of the measured ((a) to (e)) and predicted ((f) to (j)) elevations on the basis of the mean beach profile (**Figure 2**) during the periods from 1991 to 1992 (a, f), from 1993 to 1994 (b, g), from 1995 to 1996 (c, h), from 1997 to 1998 (d, i), and from 1999 to 2000 (e, j). See **Figure 5** for further explanation.



**Figure 13** Measured (solid circles) and predicted (open circles) centers of areas above the mean beach profile during the periods from 1991 to 1992 (a), from 1993 to 1994 (b), from 1995 to 1996 (c), from 1997 to 1998 (d), and from 1999 to 2000 (e).



**Figure 14** Time series of BSSc. The black, solid red, broken red, solid blue, broken blue and green lines show the values during the periods from 1991 to 1992, from 1993 to 1994, from 1995 to 1996, from 1997 to 1998, and from 1999 to 2000.

#### 7. Discussion

#### 7.1 Sediment transport rate

The seaward suspended transport rate  $Q_s$  was relatively large at the bar crest and shoreward of P150m (Figure 15). In particular, it was large when the bar migrated seaward, which would suggest that the seaward suspended load made a major contribution to the seaward migration of the bar.

The shoreward bed load  $Q_{b,v}$ , mainly induced by near-bottom velocity skewness, was also large at the bar crest and shoreward of P150m as with the suspended load, whereas the shoreward bed load induced by near-bottom acceleration skewness  $Q_{b,a}$  was large near the shoreline. The bed load due to the beach slope  $Q_{b,slope}$  was smaller than the three transport rates mentioned above.

# 7.2 Sensitivities of calibration results to calibration period and error function

#### (1) Calibration period

To investigate the influence of the calibration period on the results, the model was calibrated with 6-month and 2-year data sets starting from January 4, 1989. The smoothing number was fixed to be 15 and the obtained parameter values were  $\alpha_1 = 1.123 \times 10^{-3}$ ,  $\alpha_2 = 9.405 \times 10^{-4} (s^2/m)$ ,  $\alpha_3 = 1.099 \times 10^{-4}$  (m s) and  $\alpha_4 = 9.239 \times 10^{-4} (s^2/m)$  for the 6-month calibration period and  $\alpha_1 = 1.144 \times 10^{-3}$ ,  $\alpha_2 = 8.595 \times 10^{-4} (s^2/m)$ ,  $\alpha_3 = 7.96 \times 10^{-5}$  (m s) and  $\alpha_4 = 7.925 \times 10^{-4} (s^2/m)$  for the 2-year period.



**Figure 15** Spatial and temporal variations of the predicted cross-shore sediment transport rate Q (a), suspended sediment transport rate  $Q_s$  (b), bed transport rate due to near-bottom velocity skewness and amplitude  $Q_{b,v}$  (c), bed transport rate due to near-bottom acceleration skewness  $Q_{b,a}$  (d) and bed transport rate due to beach slope  $Q_{b,slope}$  (e). Positive values, shown by warm colors, represent seaward transport rates.

In the case of the 6-month calibration period, the predicted profiles were flattened more quickly than the profiles calibrated with the 1-year calibration period used in this study, and in May 1990, the bar predicted in the model was shown to decay (**Figure 16**). In the case of the 2-year calibration period, on the other hand, although *BSS* values in the region between



**Figure 16** Time series of bar crest positions predicted with 6-month (red solid circles) and 2-year (green solid circles) calibration periods. See **Figure 4** for further explanation.



**Figure 17** Time series of the model skill score *BSS* for 6-month (red lines) and 2-year (green lines) calibration periods. See **Figure 8** for further explanation.

P-65m and P355m were lower in 1989 and higher in 1990 than those in the 1-year calibration period (**Figure 17**), the bar crest positions predicted with the 2-year and 1-year calibration periods agree well (**Figure 16**). These results suggest that the model used in the combination with the 6-month calibration period cannot predict the cyclic bar migrations quantitatively, but the model used in conjunction with the 2-year calibration period is successful in doing so. In order to reproduce cyclic bar migrations, a calibration period covering at least one bar migration cycle, composed of bar formation, development and decay, is recommended.

#### (2) Error function

To investigate the influence of the error function, which was defined by Equation (31) as the sum of the errors in elevation and bar crest position, the calibration results with two error functions were compared. One error function was composed only of the relative error in elevation, whereas in the second error function the weight of the relative error in bar crest position was doubled. The smoothing number was fixed to be 15. The obtained parameter values for the former error function were  $\alpha_1 = 1.159 \ge 10^{-3}$ ,  $\alpha_2 = 7.27 \ge 10^{-4} (s^2/m)$ ,  $\alpha_3 = 9.94 \ge 10^{-5} (m s)$  and  $\alpha_4 = 8.189 \ge 10^{-4} (s^2/m)$ , whereas those for the latter error function were the same as those obtained through the standard calibration procedure as shown in **4.2**.

Although the decay of the bar as predicted with the parameter set for the former error function is slightly earlier than that for the error function defined by Equation (31), both bar crest positions agree well with the observations (**Figure 18**). The *BSS* value for the former error function is close to that for the error function defined by Equation (31) (**Figure 19**). These results, as well as the fact that the parameter values obtained with the latter error function are the same as those obtained through the standard calibration procedure, indicate that the calibration result in this study was not strongly



**Figure 18** Time series of the model skill score *BSS* for error function composed only of relative error in elevation (red lines). See **Figure 8** for further explanation.



**Figure 19** Time series of bar crest positions calibrated with error function composed only of relative error in elevation (red solid circles). See **Figure 4** for further explanation.

sensitive to the error function.

# 7.3 Sensitivities of prediction results to parameter values and initial beach profile

#### (1) Parameter values

Sensitivity tests were conducted by changing the  $\alpha_1$  to  $\alpha_4$ parameter values by 10% in the model predictions. The parameter to which the modeling results were most sensitive was the value of  $\alpha_1$  for suspended load. The bar predicted in the model migrated more quickly with a 10% increase in  $\alpha_1$ and more slowly with a 10% decrease, and the differences between the bar crest positions predicted with the altered  $\alpha_1$ and those predicted with the optimal  $\alpha_1$  at the end of the calibration period (December 1989) were approximately 50 m (Figure 20). The parameter to which the results showed second greatest sensitivity was the value of  $\alpha_4$  for bed load due to beach slope; the differences in the bar crest position with the altered parameter values were 25 m (Figure 21). Parameters  $\alpha_2$  and  $\alpha_3$  for bed load due to velocity and acceleration skewness, respectively, exerted the least influence on the model predictions.



**Figure 20** Bar crest positions with  $\alpha_1$  increased (red circles) and decreased (green circles) by 10 %. See **Figure 4** for further explanation.



**Figure 21** Bar crest positions with  $\alpha_4$  increased (red circles) and decreased (green circles) by 10 %. See **Figure 4** for further explanation.

(2) Initial beach profile

To examine whether the model's predictions of beach profile are dependent on the initial condition, as in deterministic chaos, the beach profile measured on January 5 and 6, 1989, were used as the initial profiles in the predictions (**Figure 22**). The standard deviations of the elevation differences from the profile on January 4 (the initial profile in



**Figure 22** Beach profiles on January 4 (thin solid lien), 5 (thick solid line) and 6 (broken line).



**Figure 23** Beach profiles predicted with initial profiles on January 4 (thin solid lien), 5 (thick solid line) and 6 (broken line).

the calibration) in the region between P-65m and P355m for profiles on January 5 and 6 were 0.12 m and 0.15 m, respectively. The result is that, although there are small discrepancies between foreshore profiles when using different initial profiles, the small differences in the initial profiles did not lead to a large difference in the prediction results (**Figure 23**). This conclusion is consistent with that of Ruessink and Kuriyama (2008).

#### 7.4 Smoothing of suspended sediment transport rate

The effect of smoothing suspended load was investigated by comparing the smoothed suspended sediment concentrations and those computed using an advection-diffusion equation of the depth-averaged suspended sediment concentration.

$$\frac{\partial(hC)}{\partial t} = \frac{\partial(hCU)}{\partial x} + \frac{\partial}{\partial x} \left( v_H \frac{\partial(hC)}{\partial x} \right) + \frac{\alpha_1 D_r}{\rho g(s-1)w_f} W - Cw_f$$
(33)

where  $v_H$  is the horizontal diffusion coefficient set to 0.1 m<sup>2</sup>/s as by Grunnet et al. (2004). The velocity of sediment suspension *W* is different from the sediment fall velocity  $w_f$  in ordinary advection and diffusion calculations. However, in this study, the suspended sediment concentration was assumed to be proportional to the surface roller energy dissipation rate, and hence the computation of the suspended sediment concentration was conducted by assuming *W* was equal to  $w_f$ .

In the computation, two representative profiles at Hasaki were used. The first was the profile measured on February 2, 1989, which included a bar crest at P185m and the second was that measured on June 2, 1989, with a crest at P310m. The input offshore significant wave heights were 1.0, 2.0 and 3.0 m and the wave period was 8.0 s. The sediment diameter was assumed to be 0.2 mm. The suspended sediment concentration value after smoothing was obtained by dividing the smoothed suspended sediment transport rate by the undertow velocity.

The peak values of smoothed suspended sediment concentration were about 1.3 to 1.7 times those computed with advection and diffusion and were located shoreward of the locations of peak in the advection and diffusion computation (**Figure 24**). However, to some extent, the smoothing of the suspended load incorporated the effects of



**Figure 24** Comparisons among suspended sediment concentrations before (thin solid lines) and after (thick solid lines) the smoothing and computed by the advection-diffusion equation (broken lines). Panels (a) to (c) show the values for the profile (d), and panels (e) to (g) for the profile (h). The deepwater wave heights are 1 m ((a, e)), 2 m ((b, f)) and 3 m ((c, g)).



Figure 25 Root-mean-square error in suspended sediment concentration versus number of smoothing.

advection and diffusion of the suspended sediment concentration into the model. Furthermore, the root-mean-square error between the smoothed and computed suspended sediment concentrations in the region between P100m and P550m was minimal with a smoothing number of 16 (**Figure 25**), which is close to the smoothing number obtained in the calibration, 15.

#### 7.5 Parameter values

The optimal parameter values were found to be  $\alpha_1 = 1.147$  x  $10^{-3}$ ,  $\alpha_2 = 7.651$  x  $10^{-4}$  (s<sup>2</sup>/m),  $\alpha_3 = 9.96$  x  $10^{-5}$  (m s) and  $\alpha_4 = 7.755$  x  $10^{-4}$  (s<sup>2</sup>/m), as mentioned in section **5.2**. The value of  $\alpha_1$ , for the suspended load, is about twice Kobayashi et al.'s (2008) value of 5.0 x  $10^{-4}$ . However, as shown above, the smoothing of the suspended load reduces the peak values, and thus the suspended transport rate estimated by the present model would be 1.5-2 times the value of Kobayashi et al. (2008).

For the bed load,  $\alpha_2$  is approximately half the value of 4.09 x  $10^{-4}$  (s<sup>2</sup>/m) used by Gallagher et al. (1998) and almost the same as the value of 6.27 x  $10^{-4}$  (s<sup>2</sup>/m) used by Hsu et al. (2006), while  $\alpha_3$  is about two-thirds the value of 1.4 x  $10^{-4}$  (m s) used by Hoefel and Elgar (2003). Although there are some discrepancies between the optimal parameter values in this study and those used in previous studies, they are in reasonable agreement.

The value for  $\alpha_4$  was assumed to be different from  $\alpha_2$  in the calibration, while both were given the same value in the study

of Bailard (1981). The optimal  $\alpha_4$  value of 7.755 x 10<sup>-4</sup> (s<sup>2</sup>/m) is almost the same as the optimal  $\alpha_2$  value of 7.651 x 10<sup>-4</sup> (s<sup>2</sup>/m).

These results along with those regarding the smoothing number in section **7.4** support the idea that the calibration was reasonably conducted.

#### 7.6 Model performance outside calibration period

Pape et al. (2009) applied data-driven models using a neural network and a process-based model to bar migrations at Hasaki. They divided the period from 1987 to 2000 into 16 blocks, each including a series of bar migrations, and predicted the bar migrations during each of the 16 blocks. Even with parameter sets optimal for each block, the performance of the model was highly variable over the 16 blocks including some blocks with very poor results. They therefore concluded that model prediction of bar migration at Hasaki was difficult.

The results of this study during the period from 1991 to 2000 (i.e., outside the period used for calibration) also show that the model skill score for the elevation *BSS*, as defined by Equation (30), was high during some periods, although *BSS* values were not necessarily high overall (**Figure 10**). Interestingly, however, measured cyclic seaward bar migrations are represented in the modeling results by the migrations of accumulation areas, which are higher than the mean beach profile. Hence, it is concluded that the model used in this study can reproduce the cycles of seaward bar evolution at Hasaki at least qualitatively.

#### 8. Conclusions

A process-based one-dimensional model for beach profile change was developed to predict cyclic bar evolutions. The model estimated beach profile change on the basis of the cross-shore gradient of the cross-shore sediment transport rate, which was assumed here to be made up of the suspended transport rate due to wave breaking and the bed transport rates due to near-bottom velocity and acceleration and beach slope.

The model was calibrated with beach profile data obtained every weekday at 5-m intervals along a 400-m-long pier at the Hazaki Oceanographical Research Station (HORS), located on the Hasaki coast of Japan, during a 1-year period from January to December 1989. In the computation, the grid size was set at 5 m and the time interval was 2 hours. The optimal values of the parameters included in the cross-shore sediment transport rate formula and the smoothing number of suspended load were obtained so that the error function denoting the sum of the relative errors in elevation and bar crest position was minimal.

The bar migrations over a period of 2 years including the 1-year calibration period of 1989 and the following year of 1990 were predicted by the model using the optimal parameter set and the optimal smoothing number. The predicted bar crest positions agreed well with those measured in the field, and the Brier skill score for elevation was above 0 by the middle of December 1990 shoreward of the tip of the pier including the foreshore, inner surf zone and bar-trough zone and over 0.5 in the bar-trough zone at the end of 1990. These results indicate that the model quantitatively predicted the cyclic bar migrations from 1989 to 1990.

The obtained optimal parameter values are 0.5 to 2 times the values used in previous studies, and hence they are thought to be in good agreement. The smoothing number of the suspended sediment transport rate was also confirmed to be effective in incorporating the influences of the advection and diffusion of suspended sediment into the model.

The model was applied to bar migrations outside the calibration period, during a 10-year period from 1991 to 2000, which was divided to five 2-year blocks. The Brier skill scores for elevation were not necessarily high for all blocks, but most of the bar crest movements detected by field measurements were expressed in the model by the movements of the areas above the mean beach profile, and the Brier skill scores for the center of the area above the mean beach profile were high for all blocks except for the 1999-2000 period. Hence, it is concluded that the model used in this study can predict cyclic bar evolutions at Hasaki even outside the calibration period at least qualitatively.

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